## CBCS SCHEME

USN			000	17CS36
Third Semester B.E. Degree Examination, Aug./Sept.2020				
Discrete Mathematical Structures				
Tim	ie: 3	hrs.		Max. Marks: 100
	N	ote: Answer any FIVE full question.	s, choosing ONE full question j	from each module.
			Module-1	
1	a.	Let p and q be primitive statements		q is false. Determine the
		truth value of the following compou	nd propositions $p \land q$ , $\neg p \lor q$ , $q$ -	
	h	Show that SVD is a toutal wimmli	od by (D. O), (D. P.) (O. S),	(07 Marks)
	U.	Show that SVR is a tautology implied	and by $(P \lor Q) \land (P \to R) \land (Q \to S)$	using rules of interence. (07 Marks)
14	c.	Define Converse, Inverse and Contr	a positive with an illustration.	(06 Marks)
			OR 🔨	
2	a.	Define tautology. Show that for any	proposition p, q, r the compoun	d propositions
* *		$[(p\rightarrow q) \land (q\rightarrow r)] \rightarrow (p\rightarrow r)$ is a		(06 Marks)
	b.	Prove the following logical equivale	^	
. a <sup>7</sup>	c.	$\{(p \rightarrow q) \land [\neg q \land (r \land \neg q)]\} \Leftrightarrow \neg$ Find whether the following argument		(07 Marks)
1. v 1.	C.	Find whether the following argumer If a triangle has 2 equal sides,		.t.
		If a triangle is isosceles, then i		
		A certain ΔABC does not have		Go)
		∴ The ∆ABC does not have 2	equal sides.	(07 Marks)
	Module-2			
3	a.	Prove by mathematical induction that		
1 3.		$1+2+3+\dots+n=\frac{1}{2}$		(08 Marks)
	b.	The Fibonacci numbers are designed	ed recursively by $F_0 = 0$ , $F_1$	$= 1, F_n = F_{n-1} + F_{n-2}$
		for $n \ge 2$ . Evaluate $F_2$ to $F_{10}$ .		(04 Marks)
	c.	Find the number of permutations of		ASAUGA. In how many
i i		of these, all 4 A's are together? How	v many of them begin with S?	(08 Marks)
	A.		OR	
4	a.	Prove by mathematical induction the	at $1^2 + 3^2 + 5^2 + \dots + (2n -$	$(-1)^2 = \frac{1}{n} n(2n-1)(2n+1)$
	1	for all integers n≥1. The I week work on a defined week.	resident - 2 I - 1 and I	(08 Marks)
	b.	The Lucas number's are defined rec Evaluate L <sub>2</sub> to L <sub>10</sub>	cursively by $L_0 = 2$ , $L_1 = 1$ and $L_2 = 1$	$L_n = L_{n-1} + L_{n-2} \text{ for } n \ge 2.$ (06 Marks)
	c.	There are four bus routes between t	the places A and B, three bus re	1
		B and C. Find the number of ways		
	. 1	does not use a route more than once		(06 Marks)
1			Module-3	
5	а	Lat f. D D by defined by gray	$\int 3x - 5  \text{for } x > 0$	
,		Let $f: R \to R$ be defined by $f(x) = \begin{cases} \begin{cases} \\ \\ \end{cases} \end{cases}$	$-3x+1$ for $x \le 0$	
	, ,	Determine f(0), f(-1), f(5/3), f <sup>-1</sup> (-1),	$f^{-1}(-3), f^{-1}(6), f^{-1}([-5, 5]).$	(07 Marks)

(06 Marks)

- b. ABC is an equilateral triangular, whose sides are of length 1 cm each. If we select 5 points inside the triangle, prove that atleast two of these points are such that the distance between then is less than ½ cm.
- c. Let  $A = \{1, 2, 3, 4\}$  and R be a relations on A defined by xRy if and only if "x divides y". written x/y. Write down R as a set of order pairs, draw the diagraph of R and determine (07 Marks) indegree and outdegree of the vertices of the graph.

- State pigeon hole principle. A bag contains 12 pairs of socks (each pair in different color). If a person drawn the socks one by one at random, determine atmost how many draws are required to get atleast one pair of matched socks.
  - 0 if x is even b. Let f, g, h be functions from z to z defined by f(x) = x - 1, g(x) = 3x, h(x) = 3x1 if x is odd

Determine (fo(goh))(x) and ((fog)oh)(x) and verify that fo(goh) = (fog)oh. c. Let,  $R = \{(1, 1), (1, 2), (1, 3), (1, 4), (2, 4), (2, 2), (3, 3), (4, 4)\}$  be relation, verify that R is a partial ordering relation or not. If yes, draw the Hasse diagram for R. (08 Marks)

Module-4

- Determine the number of positive integers n such that  $1 \le n \le 100$  and n is not divisible by (07 Marks) 2, 3 or 5.
  - (05 Marks) b. Find the number of derangements of 4, 2, 3, 4 and list them.
  - c. The number of virus affected files in a system is 1000 (to start with) and this increases by 250% every two hours. Use a recurrence relation to determine the number of virus affected (08 Marks) files in the system after one day?

- In how many ways can the 26 letters of the English alphabet be permuted so that none of the patterns CAR, DOG, FUN or BYTE occurs?
  - b. An Apple, a Banana, a Mango and an Orange are to be distributed to four boys B1, B2, B3, B4. The boys B1 and B2 do not wish to have Apple, the boy B3 does not want Banana or Mango and B4 refuses orange. In how many ways the distribution can be made so that no (07 Marks) boy is displeased?
  - c. Solve the recurrence relation

$$a_n - 6a_{n-1} + 9a_{n-2} = 0$$
 for  $n \ge 2$ , given that  $a_0 = 5$ ,  $a_1 = 12$ . (05 Marks)

- Define Isolated vertex, complete graph, Trail path with example. (06 Marks)
  - Explain Konigsberg bridge problem. (07 Marks)
  - Using the mergesort method, sort the list

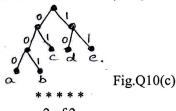
(07 Marks) 7, 3, 8, 4, 5, 10, 6, 2, 9

If G(V, E) is a simple graph, prove that 10

> $2|E| \leq |V|^2 - |V|$ (06 Marks)

b. Prove that a tree with n vertices has n-1 edges.

c. Obtain the prefix code represented by the following labeled complete binary tree shown in Fig.Q10(c) and also find the code for the words abc, cdb, bde. (08 Marks)



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